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# Multi-artery, heat pipe spreader

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#### ABSTRACT

Multiple, columnar liquid vapor chamber allows for effective heat removal from finite, concentrated heat source by heat spreading via lateral vapor flow, while minimizing conduction resistance through thinner evaporator wick. The individual liquid arteries are designed by wick coated solid pillar. We optimize the artery geometry, numbers, and distribution, for both liquid and air-cooled, finned condensers, and show that the overall thermal resistance is substantially lower than the uniform wick vapor chamber.

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## 1. Introduction

With smaller and faster microprocessors, heat removal from such concentrated sources pose challenges [1]. Using single-phase gas or liquid cooling, this concentrated heat should be spread over a sufficiently large area. Vapor chambers spread heat from concentrated sources to large condenser area, where it can be readily removed with high single-phase coolant streams. Vapor chamber (VC) is particularly effective in absence of any solid heat spreader added to the heat source (called internal heat spreader), where VC reduces the external coolant thermal resistance (due to the large area). The internal resistance of VC should be small enough such the overall thermal resistance  $R_{\Sigma}$  is small compared with no VC present.

The analysis of heat, vapor, and liquid flows in the asymmetric flat heat pipes are presented in [2] and a simplified conduction-based model for VC is given in [3], including the effect of gravity. The uniform wick VC [4] is easy to fabricate since it has a single, uniform liquid wick artery; however, it has a large conduction wick resistance. In [4] a centered, single wick column is placed above the heater area to circulate the liquid and ensure the structural stability VC. It decreases the distance of the liquid travels from condenser to evaporator, thus the evaporator wick thickness is reduced. However, it is also important to secure enough evaporation area to increase the heat flux through the wick. In [5] the measured and predicted heat flux in various modulated-wick heat pipes are presented and compared. One of models depicted as an artery-evaporator system with completely separated liquid and

vapor flow paths, and this is similar to the multiple-artery heat pipe spreader proposed here.

We design a multiple artery VC to supply liquid for evaporation and reduce the evaporator wick thickness (where its conduction resistance is dominating). The geometric parameters such as artery diameter, numbers, and spacings, are optimized based on three-dimensional resistance network analyses for heat and fluid flows. We use external, air or water cooled, finned condenser and compare the overall thermal resistance with the uniform artery VC.

### 2. Multi-artery heat pipe spreader

The multi-artery heat pipe spreader (MAHPS) is a columnar vapor chamber heat pipe. An individual artery is designed by a solid pillar covered with a uniform wick as the liquid artery. This capillary artery draws the liquid from the condenser to the evaporator wick. Water is used as an operating fluid to achieve high capillary pressure (surface tension) and heat of vaporization. Fig. 1(a) and (b) shows the geometric parameters of MAHPS, and heat flow path from the heating source to the external, coolant. MAHPS is placed between the heater area and this external heat sink. The heat source is a constant heat flux condition and the coolant is far-field temperature and surface-convection resistance surface. Since the two temperatures for the  $T_h$  and  $T_c$  are predefined as constant, isothermal heat flux and constant coolant temperature boundary conditions, respectively, in this theoretical analysis, the saturation temperature depends on how much heat spreading occurs as the heater area. Phase change occurs at the liquid-vapor interface in the evaporator and condenser wicks [6]. During the phase change, the generated vapor moves toward the condenser, where it is uniformly condensed over a large area. Capillary pressure is used for

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Nomenclature							
Α	(cross-section) area (m²)		Subscripts				
$c_p$	specific heat (J/kg-K)		atmosphere				
Ď	diameter (m)	b	bare area				
d	(fin or column) diameter (m)	С	capillary or column or condenser or coolant				
$\Delta h_{ m lg}$	enthalpy of vaporization (J/kg)	c,c	center to center				
K	permeability (m <sup>2</sup> )	e	evaporator				
k	thermal conductivity (W/m-K)	eff	effective				
L	distance or height (m)	f	fin				
M	mass flow rate (kg/s)	g	vapor				
N	number	h	heater				
$Nu_d$	Nusselt number for coolant stream, crossflow over cyl-	hex	hexagonal unit cell				
	inder	i, j	node position				
p	pressure (Pa)	k	conduction				
Pr	Prandtl number	ku	surface-convection				
Q	heat transfer rate (W)	1	liquid				
R	resistance (K/W)	lg	phase change or saturation				
$\langle Re_{\rm d} \rangle$	Reynolds number for coolant, crossflow over cylinder	MA	multi-artery heat pipe spreader				
r	radius (m)	max	maximum				
T	temperature (K)	min	minimum				
и	velocity (m/s)	p	particle				
		ps	pillar spacing				
Greek s	ymbols	S	surface or solid				
$\epsilon$	porosity	sh	superheat				
η	efficiency	$\Sigma$	overall (thermal resistance)				
$\mu$	viscosity (Pa-s)	UA	uniform-artery heat pipe spreader				
$\rho$	density (kg/m³)	VC	vapor chamber				
$\sigma$	surface tension (N/m)	W	wick				

the liquid circulation in MAHPS [7,8]. The critical geometric parameters of the baseline MAHPS are given in Table 1. For the baseline model, the heater diameter is 1 cm, and the condenser diameter is 5 cm. The wick covers the entire internal surface, including the evaporator wall and column walls, but different wick diameter, large sintered particles are used for the condenser and column, and small particles for the evaporator. In the baseline, the condenser-column and evaporator particle diameters are 200 and 50 μm, respectively. A hexagonal unit cell is used to calculate the axial and lateral heat flows, as well as the liquid pressure distribution. The thermophysical properties are evaluated at the saturation temperature of vapor which varies from 71.8 to 76.2 °C in the VC. The smaller the heater area, the lower the saturation temperature is (because of heat spreading). The effect of liquid convection in the thermal network is neglected (assuming small Péclet number [9]). In [6] the liquid and heat flow network models are designed for the steady-state analysis of the modulated wick heat pipe, and similar approach is used here.

# 3. Analysis using resistance thermal/hydraulics networks

## 3.1. Liquid flow resistance network

For the liquid flow network, the mass flow rates,  $\dot{M}_{\rm l,e}$  and  $\dot{M}_{\rm l,c}$  are calculated for each hexagonal unit cell (Fig. 1(a)). Assumptions for the network model are (i) liquid velocity is locally averaged, (ii) pressure drop by gravity is neglected, (iii) flow is Darcian and incompressible, (iv) liquid-vapor interface is in thermal equilibrium, (v) wick is isotropic, and (vi) condensation and evaporation occur on the wick surfaces [6]. Fig. 2(a) and (b) shows the thermal-hydraulic resistance network models. The liquid moves between the condenser wick and the evaporator wick. Evaporation on the evaporator wick surface is sustained by adjusting the capil-

lary pressure by reducing the effective meniscus radius there. Since the condenser has the highest liquid pressure and we assume that in the outmost location on the condenser wick the capillary pressure is zero (i.e.,  $p_{\rm l} = p_{\rm lg}$ ). The radii difference between the evaporator and condenser gives the capillary pressure difference Young–Laplace equation [8]

$$\Delta p_{\rm c} = \Delta p_{\rm l} = \frac{2\sigma}{r_{\rm c.e}} - \frac{2\sigma}{r_{\rm c.c}},\tag{1}$$

we have assumed uniform vapor pressure  $p_{\rm g}=p_{\rm lg}$ , where  $p_{\rm lg}$  is the saturation pressure.  $\sigma$  is the surface tension,  $r_{\rm c.e}$  and  $r_{\rm c.c}$  are the meniscus radii at evaporator and condenser wick surfaces. We assume  $r_{\rm c.c}$  is infinity at the outmost corner of the condenser, and the maximum capillary pressure  $p_{\rm c.max}$  is [8]

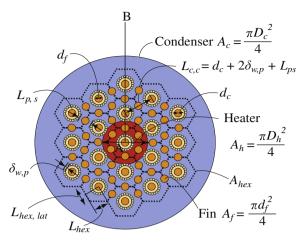
$$p_{\rm c,max} = p_{\rm g} - p_{\rm l,min} = \frac{2\sigma}{r_{\rm c,min}} \cos\theta_{\rm c}, r_{\rm c,min} = (0.41)0.5 d_{\rm p,e}, \eqno(2)$$

where the  $\theta_c$  is the contact angle and  $d_{p,e}$  is the wick particle diameter for the evaporator wick. Here,  $r_{c,min}$  is the minimum meniscus radius in Eq. (1) for sintered-particle wicks [10]. The material properties and relations are given in Table 2. Assuming that the liquid (1) and vapor (g) flow are incompressible (ii), the continuity equations are

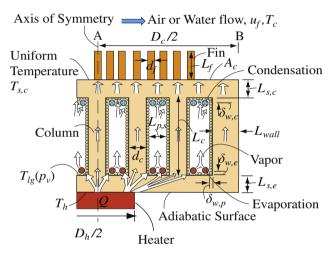
$$\nabla \cdot u_1 = 0$$
 and  $\nabla \cdot u_g = 0$ , (3)

where  $u_{\rm l}$  and  $u_{\rm g}$  are the liquid and vapor velocity vectors. The liquid mass flow rate is determined by heat flow from the constant, isothermal area, using the heat of evaporation  $\Delta h_{\rm lg}$ 

$$\dot{M_{\rm l}} = \frac{Q}{\Delta h_{\rm lg}} = \int_{A_{\rm lg}} \dot{m}_{\rm lg} \, \mathrm{d}A, \tag{4} \label{eq:mlg}$$



# (a) Top view of MAHPS



(b) Side view of MAHPS

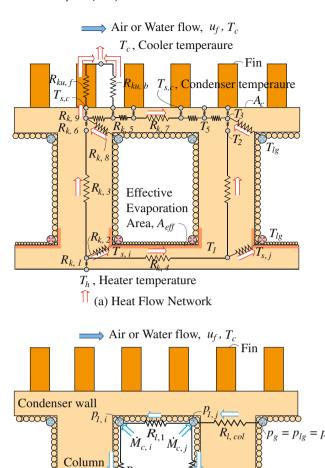
**Fig. 1.** Schematic of hexagonal unit cells around each column. (a) The size of each unit hexagonal cell varies with the column (pillar) diameter  $d_{\rm p}$ , column wick thickness  $\delta_{\rm w,p}$ , and column spacing  $L_{\rm cc}=d_{\rm c}+2\delta_{\rm w,p}+L_{\rm p.s}$ . The heater diameter  $D_{\rm h}$  is also shown. (b) The cross-sectional area of MAHPS shows the heat flow paths as well as the geometric parameters.

**Table 1**Geometric parameters for the baseline MAHPS design

Geometric parameter	Magnitude
Heater diameter, D <sub>h</sub>	1 cm
Condenser diameter, D <sub>c</sub>	5 cm
Evaporator wall thickness, $L_{s,e}$	1 mm
Condenser wall thickness, L <sub>s,c</sub>	1 mm
Side wall thickness, L <sub>s,wall</sub>	1.5 mm
Evaporator wick particle diameter, $d_{p,e}$	50 μm
Condenser wick particle diameter, $d_{p,c}$	200 μm
(Uniform artery) wick particle diameter, $d_p$	100 μm
Evaporator wick thickness, $\delta_{w,e}$	50 μm
Condenser and column wick thickness, $\delta_{w,c}$	200 μm
(Uniform artery) wick thickness, $\delta_{\rm w}$	800 μm
Column diameter, $d_c$	1 mm
Column height, L <sub>c</sub>	3 mm
Fin diameter, $d_{\mathrm{f}}$	1 mm
Heat sink coolant number of fins (water), $N_{\rm f}$	279

where  $m_{\rm lg}$  is the local evaporation flux. Using the Darcy' law [11], the liquid pressure drop is

$$\Delta p_{\rm l} = \frac{\mu_{\rm l} L}{\rho_{\rm l} KA} \dot{M}_{\rm l}, \tag{5}$$



(b) Liquid Flow Network

Evaporator wall

**Fig. 2.** Resistance network model for the thermal–hydraulic resistances assigned to each node per hexagonal unit cell. (a) The thermal resistances between adjacent temperature nodes. (b) In the wick structures, the hydraulic resistances are used between adjacent pressure nodes. The condensation and evaporation surfaces are also shown.

**Table 2**Materials properties and relations used in heat and liquid flow network models (vapor chamber fluid: water)

Properties	Symbol	Magnitude/relations
Wick porosity	$\epsilon_{\mathrm{e}}$	0.3
	$\epsilon_{ m c}$	0.4
Thermal conductivity	$k_{\rm s}$	378 W/m-K
	$k_{w}$	0.66 W/m-K
	k <sub>air</sub>	0.0287 W/m-K
	$\langle k_{\rm e} \rangle$ (wick)	0.0287 W/m-K $k_{\rm w} \left(\frac{k_{\rm s}}{k_{\rm w}}\right)^{0.28-0.757\log_{10}\epsilon_{\rm e}-0.057\log_{10}\frac{k_{\rm s}}{k_{\rm w}}}$
	[10] $\langle k_{\rm c} \rangle$	$k_{\rm W} \left(\frac{k_{\rm s}}{k_{\rm w}}\right)^{0.28 - 0.757 \log_{10} \epsilon_{\rm c} - 0.057 \log_{10} \frac{k_{\rm s}}{k_{\rm w}}}$
Contact angle for water on copper	$\theta_{\rm c}$	U
Capillary pressure	$p_{\rm c}$	$\frac{2\sigma}{(0.41)0.5d_{0.6}}$
Permeability	K <sub>e</sub> [12]	$\frac{\frac{2\sigma}{(0.41)0.5d_{p,e}}}{(0.41d_{p,e})^2} \frac{4\epsilon_e^3}{180(1-\epsilon_e)^2}$ $(0.41d_{p,c})^2 \frac{\frac{4\epsilon_e^3}{180(1-\epsilon_e)^2}}{180(1-\epsilon_e)^2}$
	$K_{c}$	$(0.41d_{p,c})^2 \frac{\epsilon_c^2}{180(1-c)^2}$
Nusselt number for crossflow over cylinders	$\langle Nu \rangle_{\rm d} \ [12]$	5.37
Prandtl number	Pr	Water: 3.22, air: 0.69
Surface-convection resistance	$R_{\mathrm{ku,c}}/A_{\mathrm{c}}$	$2 \times 10^{-5} \text{ K/W-m}^2$

where  $\mu_{\rm l}$  is the liquid viscosity, L is the flow path length,  $\dot{M}_{\rm l}$  is the liquid mass flow rate, and  $\rho_{\rm l}$  is the liquid density, K is the wick permeability determined from the Carman–Kozeny relation [12] listed in Table 2, and A is the cross-section area of the wick.  $\Delta p_{\rm l}$  should be less than the maximum capillary pressure  $p_{\rm c,max}$  (i.e.,  $\Delta p_{\rm l} \leqslant p_{\rm c,max}$ ).

### 3.2. Heat flow resistance network

The assumptions for the heat flow resistance network are (i) local thermal equilibrium between solid and liquid in the wick, (ii) condensation occurs uniformly on the condenser surface, and (iii) vapor temperature (pressure) is uniform. The energy equation is

$$\nabla \cdot \mathbf{q} = 0, \tag{6}$$

under steady-state condition. The overall heat flow rate into the evaporator is

$$Q = \int_{A} (\boldsymbol{q} \cdot \boldsymbol{s}_{n}) \, \mathrm{d}A = \dot{M}_{\mathrm{lg}} \Delta h_{\mathrm{lg}}, \tag{7}$$

where  $\mathbf{s}_n$  is the surface normal unit vector and  $A_{\mathrm{e}}$  is the evaporation area. Due to low liquid velocity in MAHPS leads to the low Péclet numbers, only conduction is considered in heat flow network. For the heat flow network, the thermal conduction resistance  $R_k$  based on one-dimensional heat conduction is

$$Q_k = \frac{\Delta T}{R_\nu}, \quad R_k = \frac{L}{kA_\nu}, \tag{8}$$

where k is the thermal conductivity,  $A_k$  is the cross-section area,  $\Delta T$  is temperature between the nodes i and j, shown in Fig. 2(a). The wick superheat  $\Delta T_{\rm sh}$  is

$$\Delta T_{\rm sh} = T_{\rm s,i} - T_{\rm lg}.\tag{9}$$

where  $T_{\rm s,i}$  is the average temperature under the evaporator wick (Fig. 2(a)). The temperature on the wick surface is the saturation temperature  $T_{\rm lg}$  and is assumed uniform within MAHPS.

# 3.3. Resistances

The liquid pressure drop in the condenser wick and the corresponding liquid resistance are

$$\Delta p_1 = \frac{\mu_l L_{p.s}}{\rho_l K_c A} \dot{M}_{l,c} = R_{l,1} \dot{M}_{l,c}, \tag{10}$$

where the cross-section area  $A=L_{\rm hex,lat}\delta_{\rm w.c}$  and  $\dot{M}_{\rm l.c}$  is the condensation rate. The arrows shown in Fig. 2(b) indicate the direction of liquid flow. The pressure drop along the column wick is

$$\Delta p_{1-2} = \frac{\mu_{l} L_{c}}{\rho_{l} K_{c} A} \left( \dot{M}_{l,c} - \dot{M}_{l,e} \right) = R_{l,1-2} \left( \dot{M}_{l,c} - \dot{M}_{l,e} \right), \tag{11}$$

where the cross-section area  $A=\pi[((d_c+2\delta_{w.e})^2-d_c^2)]/4$ ,  $\dot{M}_{l.e}$  is the liquid evaporation rate in the evaporator wick. The evaporator pressure drop is

$$\Delta p_2 = 0.25 \frac{\mu_l L_{p,s}}{\rho_l K_e A} \dot{M}_{l,c} = R_{l,2} \dot{M}_{l,c}, \tag{12}$$

where the cross-section area  $A=\pi[(d_c+2\delta_{\rm w,c})\delta_{\rm w,e}]/2$  and the evaporation is assumed to occur over 1/4 of  $L_{\rm p,s}$ . This is a simplifying assumption noting the liquid spreads short distance over the evaporator. More elaborate model may allow for local evaporation over a network preceding this region, but is not pursued here. The liquid resistance  $R_{\rm l,col}$  shown in Fig. 2(b) across column is given as

$$R_{l,col} = 0.5 \frac{\mu_l (R_c - N_r L_{hex})}{\rho_l K_c A}, \tag{13}$$

where the  $N_{\rm r}$  is the number of rings of hexagonal unit cell, and the liquid path is determined from  $N_{\rm r}$ . Here, A is the cross-section area of the inter-column defined as  $A=\pi(D_{\rm e}+N_{\rm r}L_{\rm hex})\delta_{\rm w,c}$ . The liquid flow rate for each hexagonal unit cell is

$$\dot{M}_{\mathrm{l},i} = \frac{\mathrm{Q}}{N_{\mathrm{hex}} \Delta h_{\mathrm{lg}}}, \tag{14}$$

where Q is the heat flow rate defined by the heat flow rate across the wick and  $N_{\text{hex}}$  is the number of hexagonal unit cells.

For the heat flow network, the entire geometry (evaporator and condenser wall, column, wick structure, and finned condenser) is included in the network. The axial and lateral heat flow resistances of VC are given as

$$R_k = \frac{L}{kA},\tag{15}$$

where L is the distance for heat flow, k is thermal conductivity, and A is the cross-section area normal to the heat flow. Since heat flows toward to the evaporator wall and the column, the resistance across the evaporator wick is defined by an effective evaporation area. As shown in Fig. 2(a), the effective evaporation area is

$$A_{\text{eff}} = 0.5\pi d_{c}L_{p,s} + \left[A_{\text{hex}} - \pi(d_{c} + 2\delta_{\text{w,e}})^{2}\right].$$
 (16)

The heat flow resistance of the finned external coolant is given next.

### 3.4. Heat sink (external coolant stream)

Fig. 1(b) shows the finned condenser top of VC. Since the surface-convection of air is less effective than water as coolant, the surface area should be increase (from the baseline which is for water). The geometric parameters are the number of fins, the diameter and the length of the fin, and the area of the condenser. The surface-convection resistance is

$$\frac{1}{R_{\text{ku,c}}} \equiv A_b N u_d \frac{k_f}{d_f} + \eta_f A_f N u_d \frac{k_f}{d_f}. \tag{17}$$

The  $Nu_d$  is given by the correlation for crossflow over cylinders [13]. The fin surface area  $A_f$  and flat area  $A_c$  and the bare area  $A_b$ , are

$$A_{\rm f} = N_{\rm f} \left( \pi d_{\rm f} L_{\rm f} + \frac{\pi d_{\rm f}^2}{4} \right), \quad A_{\rm c} = \frac{\pi D_{\rm c}^2}{4}, \quad A_{\rm b} = A_{\rm c} - N_{\rm f} \left( \frac{\pi d_{\rm f}^2}{4} \right).$$
 (18)

The same heat flow rate through MAHPS is removed through the finned condenser, i.e.,

$$Q = \frac{T_h - T_c}{R_{\Sigma}},\tag{19}$$

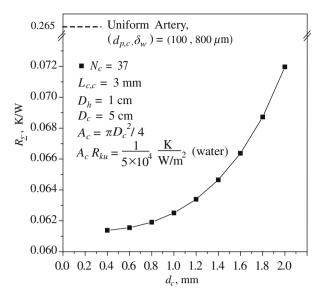
where the overall resistance,  $R_{\Sigma}$  is given in Table 4. Here, we use  $\eta_{\rm f}=1$  (i.e., relatively short fins).

### 4. Result and discussion

We now proceed to minimize  $R_{\Sigma}$  for MAHPS, and make comparison with the single, uniform artery performance.

# 4.1. Effect of internal column geometry

Fig. 3 shows the variation, as a function of artery diameter  $d_{\rm c}$ , for  $L_{\rm c,c}=3.0$  mm, and  $D_{\rm h}=1$  cm. As the diameter is reduced,  $R_{\Sigma}$  decreases. Although the thermal conductivity of the solid portion of the column (copper) is higher than the wick (sintered copper particle), the dominant heat transfer occurred is towards the evaporation surface. Increase in  $d_{\rm c}$  also reduce the evaporation area. So MAHPS performance improves when the evaporation area is increased by reducing  $d_{\rm c}$ . However, there is a minimum column



**Fig. 3.** The overall thermal resistance for MAHPS, as a function of column diameter. The overall thermal resistance for the uniform artery is also shown.

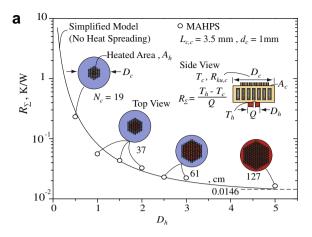
diameter, to avoid liquid chocking through the columns. The pressure drop is limited by the maximum capillary pressure, and this occurs when the column diameter is less than 0.4 mm. In addition, the conduction resistance through the column sharply increases and  $R_{\Sigma}$  increases, for  $d_c \leq 0.4$  mm. As shown in Fig. 3, the thermal resistance is inversely proportional to the evaporation area until the liquid pressure drop reaching the maximum capillary pressure. The uniform, single artery has no columns, so it has more evaporation area compared to MAHPS. However, its overall thermal resistance is about four times higher than MAPHS, due to its thick wick to avoid liquid chocking limit. Since the liquid path from condenser to evaporator in the uniform artery is longer than MAHPS, its liquid pressure drop along the wick is higher than MAHPS. Thus, the evaporator wick thickness should increase to avoid dryout and the wick conduction resistance increases. These comparisons are also listed in Table 3.

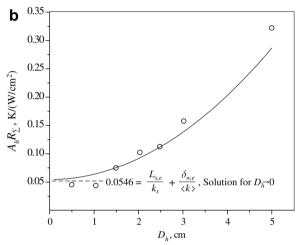
# 4.2. Effect of heater size

Fig. 4 shows the variation of overall thermal resistance with respect to the heater diameter. Here, a simplified model is used to predict maximum and minimum bounds of  $R_{\Sigma}$ , where one-dimensional heat flow (no heat spreading in the evaporator wall and wick, and no area reduction due to presence of columns) is assumed. The simplified model is

Overall thermal resistance  $R_{\Sigma}$  for various internal column diameter ( $L_{c,c}$  = 3.0 mm)

MAHPS	d <sub>c</sub> (mm)	$R_{\Sigma}$ (K/W)
$L_{\rm c,c} = 3 \text{ mm}$	0.4	0.0614
$N_{\rm c} = 37$	0.6	0.0616
$\delta_{w,p} = 200  \mu \text{m}$	0.8	0.0619
$\delta_{\rm w,c} = \delta_{\rm p,c} = 200 \ \mu {\rm m}$	1.0	0.0625
$\delta_{w,e} = \delta_{p,e} = 50 \ \mu m$	1.2	0.0634
	1.4	0.0646
	1.6	0.0664
	1.8	0.0687
	2.0	0.0720
Uniform artery	$\delta_{\rm w}$ (mm)	
$L_{c,c} = 3 \text{ mm}$	0.8	0.265

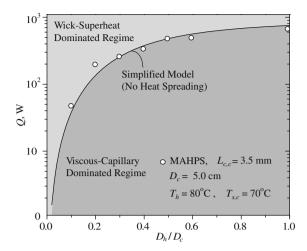




**Fig. 4.** (a) Comparison overall thermal resistance of MAHPS (axial and radial network model) with the simplified model (based on the one-dimensional network), a function of heater diameter. The number of columns indicates the heat spreading in the radial direction. (b) Same for the thermal resistance multiplied by the heater area. The asymptotic thermal resistance for small heater area is also shown

$$R_{\Sigma} = \frac{1}{A_{h}} \left( \frac{L_{s,e}}{k_{s}} + \frac{\delta_{w,e}}{\langle k_{e} \rangle} \right) + \frac{1}{A_{c}} \left( \frac{L_{c}}{k_{v}} + \frac{\delta_{w,c}}{\langle k_{c} \rangle} + \frac{L_{s,c}}{k_{s}} + \frac{A_{c}}{R_{ku,c}} \right), \tag{20}$$

where  $A_h$  is heater area where the constant, isothermal heat flux boundary condition is applied,  $L_{s,e}$  is evaporator wall thickness,  $\delta_{\rm w,e}$  and  $\delta_{\rm w,c}$  are evaporator and condenser wick thicknesses,  $A_{\rm c}$  is surface area of condenser,  $L_c$  is the distance between evaporator area and condenser wick, and  $R_{\rm ku,c}$  is the surface-convection resistance of coolant stream.  $k_v$  of  $10^5$  W/m-K is used since the thermal resistance of evaporated vapor is negligibly small [3]. From Eq. (20), the minimum of  $R_{\Sigma}$  is 0.0146 K/W, when the heater has the same size of the condenser.  $R_{\Sigma}$  is larger than this lower limit for MAHPS, shown in Fig. 4. The top view shows the number of columns when the total Q is maximized. For small  $D_h$ , the area covered by columns is relatively larger than the heater area, which implies heat spreading. As the aspect ratio of the heater and evaporator, or the thickness of the evaporator wall, is increased, more spreading occurs in the evaporation area and  $R_{\Sigma}$  increases due to this heat spreading [1]. For  $D_h < 1.5$  cm diameter, MAHPS  $R_{\Sigma}$  is less than the simplified model. This implies that the bottleneck for reducing the overall thermal resistance is the thermal resistance through the evaporator wall and wick. However, for  $D_h > 1.5$  cm, heat spreading near the heater does not contribute to the thermal resistance. It indicates that the external coolant resistance play a large role in  $R_{\Sigma}$ . Fig. 5 shows the amount of heat transferred through MAHPS, as a function



**Fig. 5.** Critical heat flow rate (dry-out limit) as a function of dimensionless heater diameter.

of  $D_{\rm h}/D_{\rm c}$ . The wick-superheat dominated regime and viscous-capillary dominated regime are marked. A maximum evaporator wick superheat of 10 °C is assumed from the pool boiling experiments [14]. The viscous-capillary limit is smaller than the superheat limit. Values of  $R_{\Sigma}$  as a function of heater diameter, are also listed in Table 4.

# 4.3. Comparison with solid copper heat spreader and uniform wick

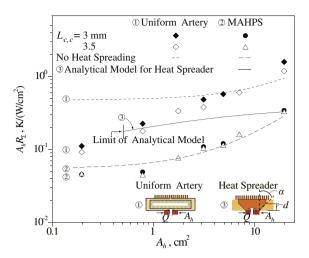
The columns in MAHPS reduce the overall flow resistance, since the condensate directly moves to the heater area. For the uniform artery, the liquid flow path is longer, this increases the overall liquid flow resistance, while its evaporation area is larger than MAHPS. Fig. 6 shows variation of  $R_{\Sigma}$  for uniform artery, MAHPS, and a solid copper heat spreader [15], as a function of  $A_h$ . For the uniform artery, the wick thickness is 800  $\mu$ m and for MAHPS, the evaporator wick thickness is 50  $\mu$ m, and this results in larger  $R_{\Sigma}$  for the uniform artery. However, there is only a small difference between the two for small  $A_h$ . Although the conduction resistance of MAHPS is less than the uniform artery, the effect of heat spreading compensates. For small heater diameter, the area for evaporation is critical. If the heater diameter is equal or smaller than the MAHPS column diameter  $d_c$ , there is no reduction in  $A_h R_{\Sigma}$  [4].

Although the vapor spreads heat uniformly, thus reducing the overall thermal resistance substantially, MAHPS may potentially be disadvantageous, compared with a solid copper heat spreader due to its low wick effective thermal conductivity. Using the analytical model for  $R_{\Sigma}$  in solid copper heat spreader [15], the results for MAHPS, uniform artery, and the solid copper heat spreader, are compared in Fig. 6. The overall (no interfacial material or resistance)  $R_{\Sigma}$  for the solid copper heat spreader is [15]

$$R_{\Sigma} = \int_{0}^{d} \frac{\cos \alpha^{-1}}{(D_{h}/2 + \tan \alpha x)^{2} \pi k_{s}} \, dx + \frac{A_{c}}{(D_{h}/2 + \tan \alpha d)^{2} \pi R_{ku,c}}, \qquad (21)$$

**Table 4** Overall thermal resistance  $R_{\Sigma}$  for the various heater diameter ( $L_{c,c}$  = 3.5 mm)

N <sub>c</sub>	$D_{\rm h}/D_{\rm c}$	D <sub>h</sub> (cm)	$A_h R_{\Sigma} (K/(W/cm^2))$	Q(W)	$\Delta T_{\rm sh}$ (°C)
19	0.1	0.5	0.0454	43.2	4.01
37	0.2	1.0	0.0438	179	3.50
	0.3	1.5	0.0749	236	3.22
	0.4	2.0	0.102	307	3.02
61	0.5	2.5	0.112	436	2.35
	0.6	3.0	0.158	449	2.25
127	1.0	5.0	0.322	610	1.13



**Fig. 6.** Comparison of the overall thermal resistance of MAHPS, the uniform artery design, and the solid copper spreader, as a function of heater area. The parameters in the solid copper spreader and the uniform artery design are also shown.

where  $\alpha$  = 70° is used as a spreading angle in the solid copper heat spreader and d is the total spreading thickness. The material properties are those listed in Table 2. Fig. 6 shows that  $A_hR_\Sigma$  for the solid copper heat spreader is lower than the uniform artery, but higher than MAHPS. Since the heat spreadability of the vapor reduces  $A_hR_\Sigma$  substantially, MAHPS shows better performance compared to the solid copper heat spreader. In Fig. 6, the simplified model for the uniform artery (no heat spreading) is differ, from the results of its network model. This is because heat spreading occurs inside the thick wick which reduces  $A_hR_\Sigma$  in network model as  $A_h$  decreases. Thus, for small  $A_h$  there is a small difference between the uniform artery and the solid heat spreader.

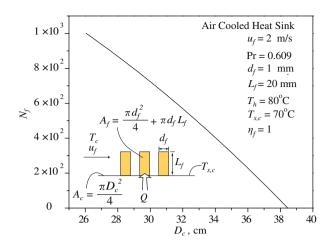
In Fig. 6,  $A_h R_\Sigma$  depends on the column spacing  $L_{c,c}$ . This implies that the size of hexagonal unit cell given by  $L_{c,c}$ , influences the accuracy of the network model results, the placement of the columns in the heater area is determined (constrained) by this unitcell size. However, this is not a large difference in  $A_h R_\Sigma$ . The numerical values used in Fig. 6 are also given in Table 5.

### 4.4. Effect of coolant

For an air cooled condenser, the number of fins and condenser diameters are found for the same cooling performance as water as the coolant ( $R_{\rm ku,c}$ ). The results are shown in Fig. 7, and compare with those of water cooled condenser (baseline design). Although air cooled condenser requires a larger surface area and number of fins, the results show a moderate condenser diameter and number of fins of the air-cooled heat sink.

**Table 5** Comparison of overall thermal resistance  $R_{\Sigma}$  between MAHPS (MA) and uniform artery (UA) design

$A_{\rm h}$ (cm <sup>2</sup> )	$N_{\rm c}$	$L_{c,c} = 3 \text{ mm}$			$L_{c,c} = 3.5 \text{ mm}$				
		$A_h R_{\Sigma,MA}$	$Q_{MA}$	$A_h R_{\Sigma,UA}$	Q <sub>UA</sub>	$A_h R_{\Sigma,MA}$	$Q_{MA}$	$A_h R_{\Sigma,UA}$	$Q_{UA}$
0.196	19	0.0454	43.3	0.111	17.7	0.0454	43.2	0.0919	20.1
0.785	37	0.0491	160	0.223	34.8	0.0438	179	0.178	22.5
1.77		_	_	_	-	0.0749	236	0.336	48.1
3.14		0.109	289	0.483	65.0	0.102	307	0.380	75.2
4.91	61	0.120	409	0.573	85.7	0.112	436	-	-
7.07		-	-	-	-	0.158	449	0.605	104
19.6	127	0.342	574	1.58	124	0.322	610	1.19	152



**Fig. 7.** Variation of predicted minimum number of fins for air cooled condenser, with respect to condenser diameter. The fin geometry is also shown.

### 5. Conclusions

In this paper, the network model for MAHPS is developed to optimize its three-dimensional heat and liquid flow. The baseline design uses water as external coolant, and air cooling is also considered. The results show while large number of columns is needed to make the most of the maximum capillary pressure by removing the most heat, the columns also limit the evaporation area. For a 1 cm diameter heater in a 5 cm diameter VC, the optimized number of columns is about 37. In addition to the viscous-capillary limit, we also use the evaporator wick-superheat limit set at 10 °C. MAHPS shows superior performance compared to the uniform artery, by reducing its overall thermal resistance.

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